Addenda

## Addenda: Van Hove Singularity and Spontaneous Fermi Surface Symmetry Breaking in Sr<sub>3</sub>Ru<sub>2</sub>O<sub>7</sub>

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In our original paper,<sup>1)</sup> we computed the uniform magnetic susceptibility  $\chi$  by employing the standard formula eq. (4). However, the magnetic susceptibility picks up an additional component, and thus its full expression should read

$$\chi = -\frac{1}{N} \sum_{\mathbf{k},\sigma} f'(\xi_{\mathbf{k}}^{\sigma}) + g \frac{\left(\frac{1}{N} \sum_{\mathbf{k},\sigma} \sigma d_{\mathbf{k}} f'(\xi_{\mathbf{k}}^{\sigma})\right)^2}{1 + \frac{g}{N} \sum_{\mathbf{k},\sigma} d_{\mathbf{k}}^2 f'(\xi_{\mathbf{k}}^{\sigma})} \,. \tag{A1}$$

This expression is obtained within random-phase approximation<sup>2)</sup> and becomes exact in the thermodynamic limit with Hamiltonian (1). The presence of the second term was overlooked in the original paper. This term yields a jump of the uniform magnetic susceptibility at a continuous phase transition and affects our results at low temperatures for  $g \neq 0$  in Fig. 3(b). Statements associated with Fig. 3(b) in the original paper should read accordingly. We here give a brief comment about the additional term in eq. (A1). The details will be published elsewhere.<sup>2)</sup>

Because of the *d*-wave form factor in the numerator of the second term in eq. (A1), this term vanishes in the symmetric phase. However, it can be finite in the symmetry-broken phase, leading to a jump of  $\chi$  at a continuous phase transition of the *d*FSD, as shown in Fig. A1. In addition, the numerator of the second term in eq. (A1) contains the spin variable  $\sigma = \pm 1$ , which imposes the necessity of breaking spin symmetry, i.e.,  $\xi_{\mathbf{k}}^{\uparrow} \neq \xi_{\mathbf{k}}^{\downarrow}$ ; otherwise, the numerator vanishes. Hence, the jump of  $\chi$  in Fig. A1 is interpreted as a field-induced anomaly. The magnitude of the jump is more pronounced at h = 0.48 than at h = 0.42, and diverges at a tricritical field ( $h \approx 0.49$ ). On the other hand, if the *d*FSD instability would occur for h = 0, for example, by tuning the chemical potential in our model (1), the second term of eq. (A1) would vanish, leading to a cusp of  $\chi$  at the *d*FSD instability, as shown in Fig. 3(b) in our original paper. Since the uniform magnetic susceptibility has not been measured thus far in the static limit for Sr<sub>3</sub>Ru<sub>2</sub>O<sub>7</sub>, the present addendum is possibly relevant to future experiments

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on Sr<sub>3</sub>Ru<sub>2</sub>O<sub>7</sub>, which can be the first system to exhibit a jump of  $\chi$  at a continuous phase transition.

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## References

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- 2) H. Yamase and P. Jakubczyk: Phys. Rev. B<br/>  ${\bf 82}$  (2010) 155119.

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Fig. A1. T dependence of  $\chi$  for two different values of h for g = 1.0; the dashed lines are results for g = 0; the choice of the parameters is the same as that in the original paper.