INCOMMENSURATE ANTIFERROMAGNETISM INDUCED BY CHARGE DENSITY MODULATION: GINZBURG-LANDAU STUDY

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In the vicinity of hole density, 1/8, of La-based high- T_c superconductors, static incommensurate antiferromagnetism (IC-AF) is observed. We explore the possible stability of static IC-AF due to the existence of static charge density modulation (CDM) using Ginzburg-Landau free energy based on the mean field theory of the t-J model. We show numerically that on the plane of hole density and incommensurability of IC-AF fluctuation, there exists a region where instability to static IC-AF is possible. In this case CDM is not necessarily a stripe pattern.

KEYWORDS: A. superconductors, D. spin density wave, D. charge-density waves, D. Fermi surface, D. magnetic properties.

1. INTRODUCTION

In the vicinity of hole density,¹ 1/8, La-based high- T_c superconductors show anomalous temperature dependence in various physical quantities such as in-plane resistivity, Hall coefficient, static magnetic susceptibility and thermoelectric power, and the following characteristics are also observed: the suppression of d-wave superconductivity (dSC); the stabilization of static incommensurate antiferromagnetism (IC-AF) with onset temperature, T_N , higher than those of other hole densities; the appearance of static charge density modulation (CDM); and the structural phase transition. We call these phenomena '1/8-phenomena'. This '1/8phenomena' has been discussed so far in the context of the stripe model first suggested by Tranquada *et al.*.^{2,3} But its justification has not been established either experimentally or theoretically.

In this paper we will investigate '1/8-phenomena' searching for possible interrelationship between the stabilization of static IC-AF and the existence of static CDM. In the following 'static CDM' will be abbreviated to 'CDM'.

2. GL FREE ENERGY

To explore the possible interrelationship between static IC-AF and CDM, we take the following Ginzburg-Landau (GL) free energy:

$$F = \sum_{q} \frac{1}{2\chi(q)} |M(q)|^{2} + \sum_{q_{a}, q_{b}} g(q_{a}, q_{b}) N(q_{a} + q_{b}) M(-q_{a}) M(-q_{b})$$

+
$$\frac{b}{4} \sum_{q_{a}, q_{b}, q_{c}} M(-q_{a}) M(q_{b}) M(-q_{b} - q_{c}) M(q_{a} + q_{c})$$
(1)

where $N(\boldsymbol{q}_a + \boldsymbol{q}_b)$ is an order parameter of CDM whose existence is assumed a priori; $M(\boldsymbol{q})$ is an order parameter of static IC-AF; $\chi(\boldsymbol{q}) > 0$ is spin susceptibility; and the second term is the lowest order interaction between static IC-AF and CDM, and $g(\boldsymbol{q}_a, \boldsymbol{q}_b)$ is the coupling constant. We consider only the static IC-AF having the same pattern as observed by neutron scattering:²⁻⁶ ($\pi, \pi \pm 2\pi\eta$) and ($\pi \pm 2\pi\eta, \pi$). η is the degree of incommensurability. In this case, CDMs which couple with this static IC-AF through the second term in eq. (1) are limited to only four patterns: 1d-CDM(I) (Fig. 1 (a)), 2d-CDM(I) (Fig. 1 (b)), 1d-CDM(II) (Fig. 1 (c)) and 2d-CDM(II) (Fig. 1 (d)). Each figure shows spin and charge patterns in the wavevector space, and η of CDM is taken as the same as that of static IC-AF. Here 1d-CDM(I) is the stripe pattern proposed by Tranquada *et al.*^{2,3}

In eq. (1) the coefficient of the second order of M(q) can change its sign when $|N(q_a + q_b)|$ becomes large. A critical amplitude of CDM, above which the sign of this coefficient becomes negative, is given by: $N_{\rm cr} = 1/(g(q_1, q_1)\chi(q_1))$ for 1d-CDM(I); $N_{\rm cr} = 2/(g(q_1, q_1)\chi(q_1))$ for 2d-CDM(I); and $N_{\rm cr} = 1/(g(q_1, q_2)\sqrt{\chi(q_1)\chi(q_2)})$ for both 1d-CDM(II) and 2d-CDM(II), where $q_1 = (\pi, \pi + 2\pi\eta)$ and $q_2 = (\pi + 2\pi\eta, \pi)$. Since the charge density must be positive, $N_{\rm cr}$ should be less than average hole density (doping rate), δ , if instability to static IC-AF occurs. Depending on the value of $a(\eta; \delta) \equiv N_{\rm cr}/\delta$, we classify three regions: (1) $a(\eta; \delta) < 1$. Static IC-AF can be stabilized by CDM (2) $a(\eta; \delta) \gtrsim 1$. CDM can not stabilize static IC-AF, but effects of CDM is still strong and will affect IC-AF fluctuations (3) $a(\eta; \delta) \gg 1$. Effects of CDM are negligible and IC-AF fluctuation is controlled only by $\chi(q)$.

3. RESULTS OF NUMERICAL CALCULATIONS BASED ON THE *t-J* MODEL

To estimate $a(\eta; \delta)$ we calculate⁷ $g(\mathbf{q}_a, \mathbf{q}_b)$ and $\chi(\mathbf{q})$ based on the mean field theory of the *t-J* model with LSCO-type Fermi surface⁸ in the singlet-RVB state at temperature, T = 0.02J, in the doping region, $0.10 \le \delta \le 0.30$. In the mean field theory $\chi(\mathbf{q}) = \chi_0(\mathbf{q})/(1+2J(\mathbf{q})\chi_0(\mathbf{q}))$ where $\chi_0(\mathbf{q})$ is spin susceptibility without interactions and $J(\mathbf{q}) = \tilde{J}(\cos q_x + \cos q_y)$ with $\tilde{J} =$ J. Phys. Soc. Jpn.

J. For explicit calculations we set $\tilde{J} = 0.2 J$ to simulate the possible effects of renormalization due to fluctuations or higher order contributions. This choice of $\tilde{J} = 0.2 J$, however, is rather arbitrary (see end of § 4).

The condition that $\chi(q) > 0$ in eq. (1) is confirmed numerically. As reported earlier,⁸ $\chi(q)$ takes a maximum at $(\pi, \pi \pm 2\pi\eta)$ and $(\pi \pm 2\pi\eta, \pi)$; we defined this η as η_{χ} . The η -dependences of $a(\eta; \delta)$ for both 1d-CDM(II) and 2d-CDM(II) are shown in Fig. 2. As a function of η , $a(\eta; \delta)$ decreases monotonically and takes a minimum at $\eta \equiv \eta_a$ then suddenly increases for $\delta \ge 0.22$, while it monotonically increases for $\delta \le 0.20$. δ -dependence of η_{χ} and η_a is shown in Fig. 3, where η_a grows rapidly around $\delta \approx 0.20$ and gets close to η_{χ} . Around the thick line in Fig. 3, $a(\eta; \delta)$ becomes less than 1. Thus both 1d-CDM(II) and 2d-CDM(II) can in principle stabilize static IC-AF.

For 1d-CDM(I), $a(\eta; \delta)$ becomes larger than that for both 1d-CDM(II) and 2d-CDM(II) about a few % ~ 10 % depending on η at each δ . For 2d-CDM(I), $a(\eta; \delta)$ is twice as large as that for 1d-CDM(I). Except for these quantitative differences, the η -dependence of $a(\eta; \delta)$ does not change among four CDMs.

4. CONCLUSION AND DISCUSSION

We have seen that both 1d-CDM(II) and 2d-CDM(II) can in principle stabilize static IC-AF more easily than 1d-CDM(I) around the thick line in Fig. 3 ($\delta \gtrsim 0.26$, $\eta \approx 0.13 \sim 0.15$). The possibility of 2d-CDM(I) is much smaller than the other CDM patterns. CDM is not necessarily a stripe pattern (1d-CDM(I)) in the present framework.

To get a global picture of how instability to static IC-AF occurs, we discuss δ -dependence of η for IC-AF fluctuation. In the absence of the coupling between N and M, η of IC-AF fluctuation is η_{χ} giving a maximum of $\chi(\mathbf{q})$ while we assume that η of CDM, η_{κ} , is equal to 1/8 resulting from some commensurability effects. In the presence of the coupling, if η_{χ} is not equal to η_{κ} and effects of coupling are strong, N and M will tend to have the same η because N couples with M having the same η . Since we have found numerically that $a(\eta; \delta) \gg 1$ for $\eta_{\chi} < \eta < \eta_{\kappa}$ while $a(\eta; \delta) \sim 1$ for $\eta_{\kappa} < \eta < \eta_{\chi}$, we expect that the resulting η of IC-AF fluctuation deviates from η_{χ} as shown by the dotted line in Fig. 3. That is, η tends to saturate at high hole density and probably crosses the thick line at $(\eta, \delta) \approx (0.13, 0.26)$, where instability to static IC-AF can occur.

This global picture is consistent with experiments^{2–6,9} qualitatively. It is noteworthy that the value of $\eta \approx 0.13$ for static IC-AF is close to the observed one, $\eta \approx 0.12$.^{2,3,5,6} But the absolute value of hole density is much larger than that of experiments. To improve this problem, the following theoretical consideration may be required: (1) effects of gauge fluctuation on the mean field solutions (2) effects of disorders (3) and ambiguity of Fermi surface.

Finally we mention the value of $\tilde{J} = 0.2J$. If \tilde{J} is taken larger, $a(\eta; \delta)$ becomes smaller and the region of the thick line in Fig. 3 extends to lower hole density.

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Fig. 1. Four possible patterns of static CDMs are represented by '•' when static IC-AF has wavevectors as shown by '×' in each figure: (a) 1d-CDM(I) has $(\pm 4\pi\eta, 0)$ or $(0, \pm 4\pi\eta)$, and the case of $(0, \pm 4\pi\eta)$ is shown (b) 2d-CDM(I) (c) 1d-CDM(II) has $(\pm 2\pi\eta, \pm 2\pi\eta)$ or $(\pm 2\pi\eta, \mp 2\pi\eta)$, and the case of $(\pm 2\pi\eta, \mp 2\pi\eta)$ is shown (d) 2d-CDM(II).



Fig. 2. The η -dependence of $a(\eta; \delta)$ for both 1d-CDM(II) and 2d-CDM(II). The case of $\delta = 0.10, 0.15$ is out of the frame and is not shown.



Fig. 3. The δ -dependence of η_{χ} and η_{a} is shown for both 1d-CDM(II) and 2d-CDM(II). Around the thick line $a(\eta; \delta)$ becomes less than 1, thus CDM can induce static IC-AF. In the absence of the coupling, IC-AF fluctuation has $\eta = \eta_{\chi}$ and we assume that η of CDM, η_{κ} , is equal to 1/8. We expect that owing to the strong coupling with CDM, η of IC-AF fluctuation deviates from η_{χ} as shown by the dotted line and crosses the thick line, where static IC-AF can be stabilized.

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