

# CRITICAL FREQUENCY OF MICROWAVE ASSISTED MAGNETIZATION SWITCHING

H. ARAI<sup>1</sup>, and H. IMAMURA<sup>2</sup>

1) AIST, Spintronics R. C., Tsukuba, Japan, and PRESTO, JST, Kawaguchi, Japan, arai-h@aist.go.jp

2) AIST, Spintronics R. C., Tsukuba, Japan, h-imamura@aist.go.jp

## I. INTRODUCTION

The microwave-assisted switching (MAS) of magnetization is a promising method for reducing the switching field of ultrahigh-density magnetic recording media [1]. The most important feature of MAS is that the switching field decreases with increasing frequency  $f$  of the radio frequency (rf) field  $H_{\text{rf}}$ , and it takes a minimum value at a certain critical frequency  $f_c$ . Although past studies based on the macrospin model in a rotating frame revealed the physics behind  $f_c$ , an analytical expression for  $f_c$  has not been obtained; i.e.,  $f_c$  was obtained only by numerical calculation. In this paper, we theoretically analyzed MAS in a perpendicularly magnetized circular disk and derived an analytical expression for  $f_c$  by analyzing the presence of a quasi-periodic mode by calculating the energy change over one precession period in the rotating frame [2].

## II. MODEL AND THEORY

Schematic illustration of the system we studied is shown in Fig. 1(a). We assumed a perpendicularly magnetized circular disk. A static magnetic field  $\mathbf{H}_{\text{dc}}$  is applied in the negative  $z$ -direction. A circularly polarized rf field  $\mathbf{H}_{\text{rf}}(t)$  is also applied in the  $x$ - $y$  plane, where the amplitude is  $H_{\text{rf}}$  and the angular frequency is  $\omega$ . We adopt a rotating frame where  $X$ - and  $Y$ - axes rotate around the  $z$ -axis, which keeps the  $X$ -axis follows the rf field as shown in Fig. 1(b). The dimensionless Landau-Lifshitz-Girbert (LLG) equation in the rotating frame is given by,

$$(1) \quad d\mathbf{m}/d\tau = -\mathbf{m} \times \mathbf{h}_{\text{eff}}^{\text{rot}} - \alpha \mathbf{m} \times (\mathbf{m} \times \mathbf{h}_{\text{eff}}^{\text{rot}}) - \alpha \omega_d \mathbf{m} \times (\mathbf{m} \times \mathbf{e}_z),$$

where  $\mathbf{h}_{\text{eff}}^{\text{rot}} = [H_{\text{rf}} \mathbf{e}_X + (-H_{\text{dc}} + H_k^{\text{eff}} m_z) \mathbf{e}_z]/M_s$ ,  $\omega_d = \omega/\gamma M_s$ ,  $\tau = \gamma M_s t$ , and  $\mathbf{e}_i$  is the unit vector along  $i$ -axis. We assume  $\alpha \ll 1$ . The effective anisotropy field is defined as,  $H_k^{\text{eff}} = 2K_u/(\mu_0 M_s) - M_s$ , where  $K_u$  is the uniaxial anisotropy constant,  $\mu_0$  is the magnetic permeability of vacuum,  $M_s$  is the saturation magnetization.

The fixed points of Eq. (1) are obtained by setting  $d\mathbf{m}/d\tau = 0$ . They are called periodic (P) modes, because the fixed points in the rotating frame represent the state rotating with  $\omega$  in the laboratory frame [3]. The stability of the P mode is analyzed by a linearized equation of motion for a small deviation of  $\delta\mathbf{m}$  from the fixed point,  $d\delta\mathbf{m}/d\tau = A\delta\mathbf{m}$ , where  $A$  is the matrix. In the simple analysis,  $f_c$  is obtained  $\det A = \text{Tr} A$  and is larger than that obtained by numerical simulations [4].

The discrepancy is solved by considering quasiperiodic (Q) modes, which represent limit cycles in the rotating frame [3]. The magnetization switching is the transition from the initial P mode to the final P mode. If an attractive Q mode exists between them, the switching is interrupted. Such Q mode appears in the lower frequency than  $f_c$  given by the simple analysis [5]. The presence of the Q mode is analyzed by calculating the change over one precession period at the saddle point of the magnetic energy density,  $d\mathcal{E}/d\tau = w_{\text{dis}} + w_{\text{rf}}$ , where  $w_{\text{dis}}$  represents the work of dissipation and  $w_{\text{rf}}$  represents the work of the rf field. By integrating over one precession period, one obtain the energy loss (gain) due to dissipation (rf field). The value of  $f_c$  is obtained by solving the equation where energy loss and energy gain are balanced,

$$(2) \quad f_c = \gamma H_k^{\text{eff}} F^{2/3} \{6 - 5F^{2/3}\} / (6\pi \{1 - F^{2/3}\}^{1/2})$$

in SI unit. Here  $F$  is  $H_{\text{rf}}/H_k^{\text{eff}}$ . For a small rf field satisfying  $H_{\text{rf}} \ll H_k^{\text{eff}}$ , the critical frequency is approximated as  $f_c \sim \gamma/\pi \{H_k^{\text{eff}} H_{\text{rf}}^2\}^{2/3}$ .

Hiroko Arai  
E-mail: arai-h@aist.go.jp  
tel: +81-29-862-6639

## III. RESULTS

Figure 1(c) shows switching field as a function of rf frequency numerically obtained from magnetization dynamics solved by LLG equation. We set initial state as  $m_z = 1$ . Applying  $H_{dc}$  and  $H_{rf}(t)$  at  $t = 0$ , magnetization dynamics is calculated for 100 ns. Then if  $m_z < 0$ , we clarified the magnetization is switched. The dots in Fig. 1(c) indicate that the magnetization is switched. Material parameters are assumed as  $M_s = 1.0$  MA/m,  $K_u = 0.85$  MJ/m<sup>3</sup>, and  $\alpha = 0.01$ . The value of  $f_c$  is found at 4.6 GHz for  $H_{rf} = 0.4$  kOe (31.8 kA/m). Figure 1(d) shows  $H_{rf}$  dependence of  $f_c$ . The dots indicate the numerical results, and dashed line indicates the analytical result calculated by Eq. (2). Our analytical expression agrees well with the numerical results.

## IV. SUMMARY

We analyzed the presence of a quasiperiodic mode for magnetization dynamics in the rotating frame, and obtained the analytical expression for the critical frequency in magnetization switching assisted by rf field. The value of  $f_c$  is expressed as a function of  $H_{rf}$  and  $H_k^{eff}$ . The validity of the analytical formula is confirmed by comparing with the numerical simulations.

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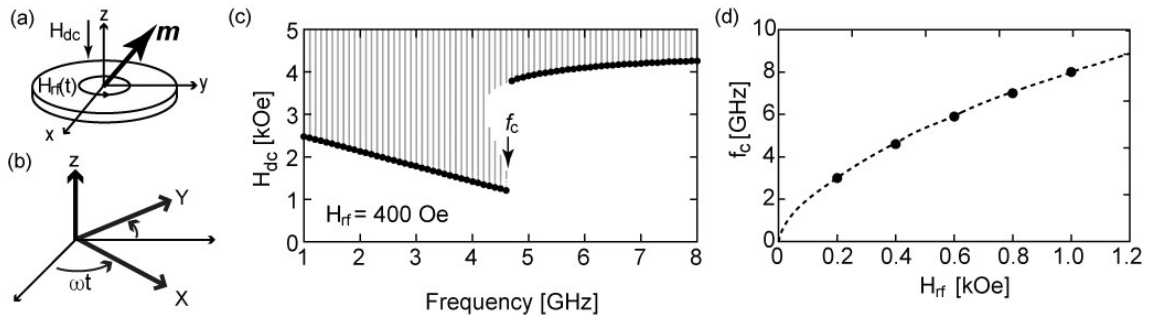


Fig. 1 (a) Schematic illustration of the circular disk and laboratory frame. (b) Definition of the rotating frame. (c) Numerically obtained switching condition. In the colored area,  $\mathbf{m}$  is switched. Critical frequency ( $f_c$ ) is indicated by the arrow. (d)  $H_{rf}$  dependence of  $f_c$ . Circles represent numerically obtained  $f_c$ . Dashed line represents  $f_c$  given by Eq. (2).